

**Aim: How do we find horizontal and vertical asymptotes?****I. Do Now:**1. What value(s) of  $x$  make each function undefined?

(a)  $f(x) = \frac{2x}{x-3}$

(b)  $g(x) = \frac{x-5}{x^2-9}$

(c)  $h(x) = \frac{8}{x^2+2}$

2. As  $x \rightarrow \infty$  or  $x \rightarrow -\infty$ , what value does each fraction approach?(Try substituting a very large number, like 1,000,000, for  $x$ .)

(a)  $f(x) = \frac{1}{x}$

(b)  $g(x) = \frac{2x^2+1}{x^2}$

(c)  $h(x) = \frac{x^2-3}{2x}$

**II. Rules for Asymptotes of Rational Functions**

*Vertical Asymptotes (VA):* There can be from 0 to an infinite number of vertical asymptotes.  
To find VA, find all values of  $x$  that make the fraction undefined.

*Horizontal Asymptotes (HA):* There is at most 1 horizontal asymptote for a rational function.

Consider the degree of the numerator and the denominator and look at their leading coefficients (i.e., the terms with the highest exponent.)

- If the degree of the numerator is less than the degree of the denominator, then \_\_\_\_\_
- If the degree of the numerator is equal to the degree of the denominator, then \_\_\_\_\_
- If the degree of the numerator is greater than the degree of the denominator, then \_\_\_\_\_

**III. Examples:** For each rational function, state the equations of all VA and HA.

3.  $f(x) = \frac{2x+1}{x+1}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

4.  $g(x) = \frac{6}{x+2}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

5.  $h(x) = \frac{-2x^3}{x^2-4}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

6.  $h(x) = \frac{2x^2}{3x^2+1}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

7.  $f(x) = \frac{2x^2}{x+\pi}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

8.  $g(x) = \frac{1-x}{x}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

9.  $g(x) = \frac{7}{x(x-2)(x-3)}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

10.  $h(x) = \frac{7x^4}{x^4-1}$

VA: \_\_\_\_\_

HA: \_\_\_\_\_

**HW36**

p. 147: 9, 10 (disregard directions; state domain and equations of VA and HA)

p. 147: 11, 12, 15

p. 141: 58