

Aim: The Parabola as a Conic Section**I. Do Now:** Recall the definition and equations below.

Definition: A parabola is the set of all points (x, y) that are equidistant from a fixed line (called the *directrix*) and a fixed point (called the *focus*) not on the line.

$$\text{Equation for Vertical Parabola: } (x - h)^2 = 4p(y - k)$$

$$\text{Equation for Horizontal Parabola: } (y - k)^2 = 4p(x - h)$$

1. Write an equation for a parabola with the given conditions. Make a sketch for each case.
- | | | | |
|------------------------|------------------------|------------------------|------------------------|
| (a) vertex at $(0, 0)$ | (b) vertex at $(0, 0)$ | (c) focus at $(-3, 5)$ | (d) focus at $(-3, 5)$ |
| focus at $(0, 4)$ | focus at $(-4, 0)$ | directrix: $y = 1$ | directrix: $x = 1$ |

II. Applications:

- | | |
|--|---|
| <p>2. Find the equation of the parabola with its vertex at $(-2, 4)$ and with directrix $y = 7$.</p> | <p>3. Find the equation of the parabola with its focus at $(2, -1)$ and with directrix $x = -2$.</p> |
| <p>4. Find the vertex, focus, and directrix of the parabola whose equation is $x^2 + 12y = 0$.</p> | <p>5. Find the vertex, focus, and directrix of the parabola whose equation is $x^2 - 4x - 8y + 28 = 0$.</p> |
| <p>6. Find the vertex, focus, and directrix of the parabola whose equation is $x = -2y^2 + 4y + 1$.</p> | <p>7. Write an equation for the parabola whose vertex is $(0, 2)$ and which passes through the points $(-2, 0)$ and $(-2, 4)$. State the coordinates of the focus and the equation of the directrix.</p> |