

**Aim: What is Cramer's Rule?****I. Do Now:**

1. Solve by Gauss-Jordan Elimination.

$$2x + 3y = 7$$

$$2x + 6y = 16$$

2. Find each determinant:

(a) 
$$D = \begin{vmatrix} 2 & 3 \\ 2 & 6 \end{vmatrix}$$

(b) 
$$D_x = \begin{vmatrix} 7 & 3 \\ 16 & 6 \end{vmatrix}$$

(c) 
$$D_y = \begin{vmatrix} 2 & 7 \\ 2 & 16 \end{vmatrix}$$

3. Use your answers from #2 to find each value:

(a) 
$$\frac{D_x}{D} =$$

(b) 
$$\frac{D_y}{D} =$$

**II. Cramer's Rule for  $2 \times 2$  Systems**

Given

$$ax + by = r$$

$$cx + dy = s$$

$$x = \text{_____} \quad y = \text{_____}$$

Try Cramer's Rule on these:

4.  $3x + 4y = -2$

$5x + 3y = 4$

5.  $7x - 7y = 8$

$-3x + 3y = 2$

6.  $-3x + 6y = 30$

$x - 2y = -10$

**III. Cramer's Rule for  $n \times n$  Systems**In general, a linear system in  $n$  variables,  $x_1, x_2, x_3, \dots, x_n$  has solutions

$$x_1 = \frac{D_{x_1}}{D}, x_2 = \frac{D_{x_2}}{D}, \dots, x_n = \frac{D_{x_n}}{D}, \text{ where } D \text{ is the coefficient matrix and } D_{x_i} \text{ is the}$$

matrix obtained by replacing the  $i$ th column of  $D$  with the "answer column."**IV. Applications:** Solve each system using Cramer's Rule. You may use your calculator to compute determinants.

7.  $2x - 3y + 4z = 1$

$x + 6z = 0$

$3x - 2y = 5$

8.  $4x + 5y - 2z = -14$

$7x - y + 2z = 42$

$3x + y + 4z = 28$

9. Find the value of  $B$  using Cramer's Rule.

$$2A - B - 3C + 2D = -2$$

$$A - 2B + C - 3D = 4$$

$$3A - 4B + 2C - 4D = 12$$

$$2A + 3B - C - 2D = -4$$