

Aim: What are some interesting polar graphs?**I. Do Now:**

(a) Convert each equation to rectangular form:

(i) $\theta = 0$ (ii) $r = \frac{3}{\sin\theta - 2\cos\theta}$

(b) Convert each point to polar form

(i) $(\sqrt{3}, -1)$ (ii) $(-1, -1)$

II. Calculator Setup for Polar Graphs

MODE: Radian, Pol(ar)

WINDOW: $\theta_{\min} = 0$, $\theta_{\max} = 2\pi$, $\theta_{\text{step}} = 0.138$ $X_{\min} = -6$, $X_{\max} = 6$, $Y_{\min} = -4$, $Y_{\max} = 4$ TABLE: Use TBLSET and TABLE to find points (r, θ) **III. Several important types of graphs have equations that are simpler in polar form than in rectangular form.**For example, the circle $r = 4\sin\theta$ has the more complicated rectangular equation $x^2 + (y - 2)^2 = 4$.

Use your graphing calculator to graph equation and sketch it below.

| | | |
|--------------------------|--------------------------|---|
| 1. $r = 3 + 2\cos\theta$ | 2. $r = 3 - 4\sin\theta$ | <u>Limaçons</u> |
| 3. $r = 4\sin 3\theta$ | 4. $r = 5\cos 2\theta$ | <u>Rose Curves</u> (What determines the number of petals?) |
| 5. $r^2 = 4\sin 2\theta$ | 6. $r^2 = 4\cos 2\theta$ | <u>Lemniscates</u> |
| 7. $r = 3\cos\theta$ | 8. $r = 2\sin\theta$ | <u>Circles</u> |

IV. Other interesting polar graphs to explore:9. $r = \theta$ ($-2\pi \leq \theta \leq 2\pi$) spiral of Archimedes10. $r^2\theta = 1$ lituus11. $r = e^\theta$ logarithmic spiral12. $r = e^{\cos\theta} - 2\cos 4\theta + \sin^5\left(\frac{\theta}{12}\right)$ butterfly curve13. $r = \cos\frac{\theta}{2}$