

Aim: A Review of Complex Numbers. What is Descartes' Rule of Signs?**I. Do Now:**

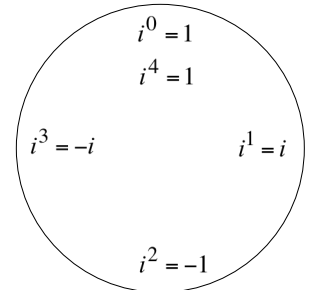
Find all roots (real and imaginary) of $f(x) = x^5 + x^3 + 2x^2 - 12x + 8$. (Note: There may be repeated roots.)

II. Recall:

i. $i = \sqrt{-1}$ and $i^2 = -1$

ii. To evaluate i^n , divide n by 4 to get remainder r ; $i^n = i^r$

iii. All numbers can be written in $a + bi$ form, i.e. as a complex number.

**III. Miscellaneous Applications**

1. Evaluate: (a) i^{57} (b) i^{720}

2. Write the conjugate of (a) $3 + 2i$ (b) $-\sqrt{3} - 4i$ (c) 3 (d) $2i$

3. Multiply and write answers in $a + bi$ form:

(a) $(-i)(3i)$ (b) $(2 - i)(3 + 4i)$ (c) $(3 + 2i)(3 - 2i)$

4. Divide and write answers in $a + bi$ form:

(a) $\frac{1}{1+i}$ (b) $\frac{4-2i}{2+3i}$ (c) $\frac{2+3i}{4-2i}$

5. Solve for x : $x^2 + 9 = -16$

IV. Descartes' Rule of Signs

René Descartes (1596 – 1650) discovered this rule: Let $f(x)$ be a polynomial with real coefficients. Then:

- The number of positive real roots of $f(x)$ is either equal to the number of variations in sign of $f(x)$ or is less than this number by a positive even integer (i.e., a multiple of 2).
- The number of negative real roots of $f(x)$ is either equal to the number of variations in sign of $f(-x)$ or is less than this number by a positive even integer (i.e., a multiple of 2).

Find the number of possible positive and negative real roots for each polynomial function:

of Positive Real Roots # of Negative Real Roots

6. $f(x) = x^6 - 3x^4 - 2x^2 + 4x - 5$

7. $f(x) = -2x^4 + x^3 - 7x^2 + 4x + 1$

8. $f(x) = 3x^3 - 4x^2 - 4x + 4$