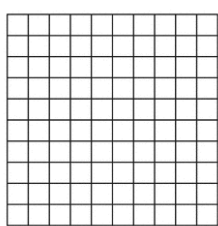


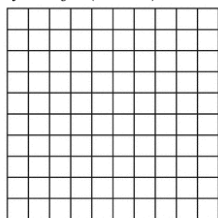
Aim: What are non-rigid transformations?

I. Do Now:

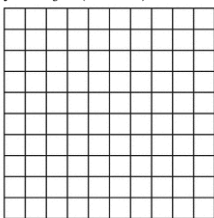
1. Given the graph of $y = f(x)$ below, graph each transformation:



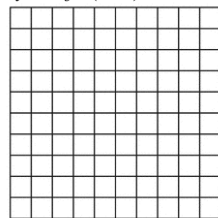
(a) $y = f(x - 1) + 2$



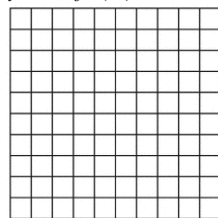
(b) $y = f(x + 1) - 3$



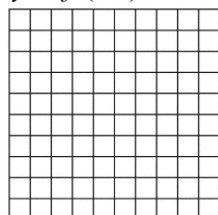
(c) $y = f(-x)$



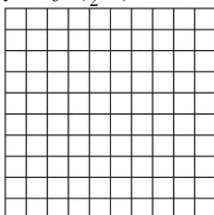
(d) $y = -f(x)$



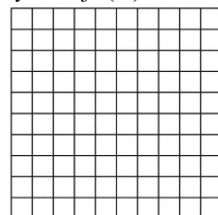
* (e) $y = f(2x)$



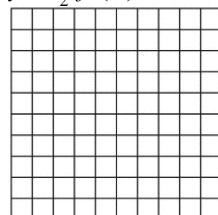
* (f) $y = f(\frac{1}{2}x)$



* (g) $y = 2f(x)$



* (h) $y = \frac{1}{2}f(x)$



II. Summary of Transformation Rules. (Assume that a represents a positive number.)

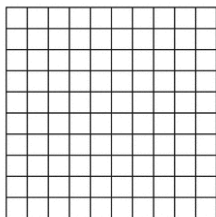
<i>Rigid Transformations</i> (size and shape are preserved)	Reflection in the x -axis	$(x, y) \rightarrow$	$-f(x)$
	Reflection in the y -axis	$(x, y) \rightarrow$	$f(-x)$
	Translation horizontally to the right	$(x, y) \rightarrow$	$f(x - a)$
	Translation horizontally to the left	$(x, y) \rightarrow$	$f(x + a)$
	Translation vertically up	$(x, y) \rightarrow$	$f(x) + a$
	Translation vertically down	$(x, y) \rightarrow$	$f(x) - a$
<i>Non-Rigid Transformations</i> (size and shape are NOT preserved)	Stretch/shrink horizontally	$(x, y) \rightarrow$	$f(ax)$ (stretches horizontally when _____) (shrinks horizontally when _____)
	Stretch/shrink vertically	$(x, y) \rightarrow$	$af(x)$ (stretches vertically when _____) (shrinks vertically when _____)

PERFORM MULTIPLE TRANSFORMATIONS IN THE FOLLOWING ORDER:

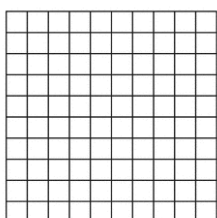
- (1) Horizontal Translation
- (2) Stretching or Shrinking
- (3) Reflecting
- (4) Vertical Translation

III. Applications.

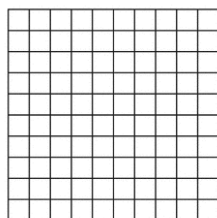
2. Sketch the graph of $f(x) = |x|$ below. Then use the rules above to sketch each transformation.



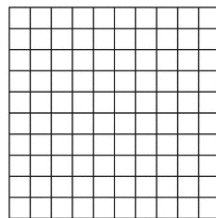
(a) $f(x) = 2|x|$



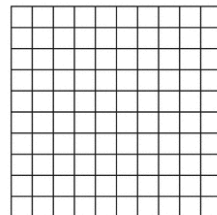
(b) $f(x) = \frac{1}{2}|x|$



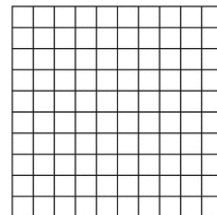
(c) $f(x) = |2x|$



(d) $f(x) = |\frac{1}{2}x|$



(e) $f(x) = |2 - x|$



(f) $f(x) = |1 - 2x| + 3$

