

MCS22 Homework 3

In 1 – 9, for each function, use calculus techniques to determine:

- (a) intervals where f is increasing and/or decreasing
- (b) coordinates of relative maxima and/or relative minima
- (c) intervals where f is concave up and/or concave down
- (d) coordinates of point(s) of inflection

1. $f(x) = x^3 - 6x^2$

2. $f(x) = x^4 - 18x^2$

3. $f(x) = (x + 1)^3$

4. $f(x) = x^4 - 8x^3$

5. $f(x) = x + \frac{9}{x}$

6. $f(x) = 3x^{2/3} - 3$

7. $f(x) = \frac{x - 1}{x + 2}$

8. $f(x) = \frac{x^2}{x^2 - 1}$

9. $f(x) = 2 + \frac{1}{(x - 1)^2}$

10. Find the absolute minimum and absolute maximum of $y = x^2 - 4$ on the interval $[-1, 3]$.

11. Find the absolute minimum and absolute maximum of $y = x^3 - 6x^2$ on the interval $[-1, 7]$.