

Name: \_\_\_\_\_

Date: \_\_\_\_\_

## GRAPHS AND ZEROES OF A POLYNOMIAL COMMON CORE ALGEBRA II



A polynomial is a function consisting of terms that all have whole number powers. In its most general form, a polynomial can be written as:

$$y = a_n x^n + a_{n-1} x^{n-1} + \cdots + a_1 x + a_0$$

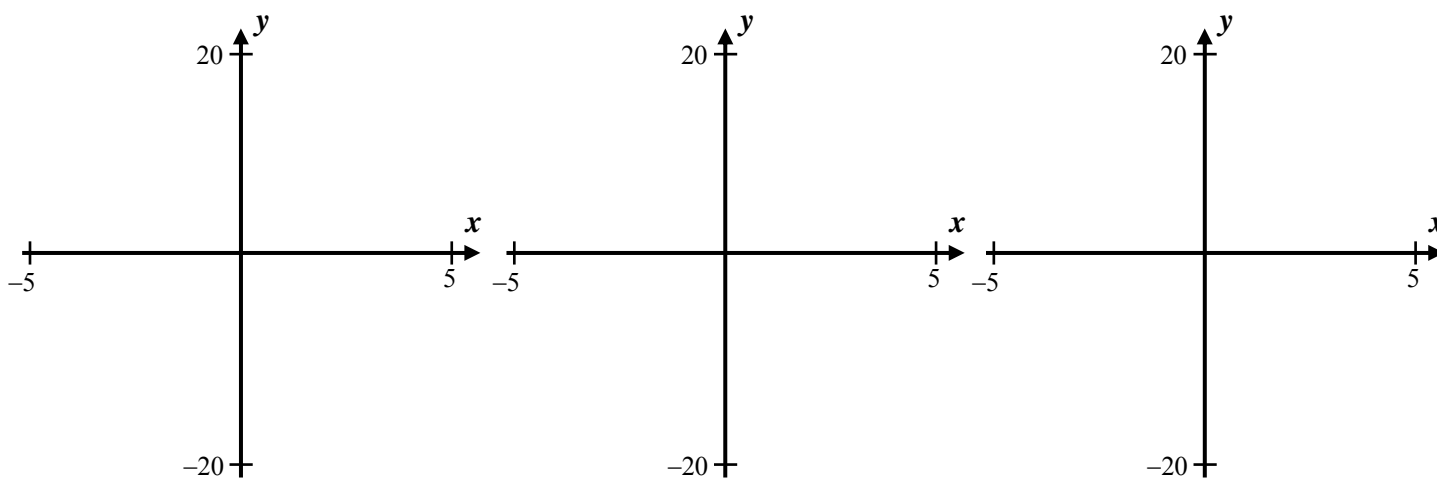
Quadratic and linear functions are the simplest of all polynomials. In this lesson we will explore cubic and quartic functions, those whose highest powers are  $x^3$  and  $x^4$  respectively.

**Exercise #1:** For each of the following cubic functions, sketch the graph and circle its  $x$ -intercepts.

(a)  $y = x^3 - 3x^2 - 6x + 8$

(b)  $y = 2x^3 - 8x + 9$

(c)  $y = 2x^3 - 12x^2 + 18x$

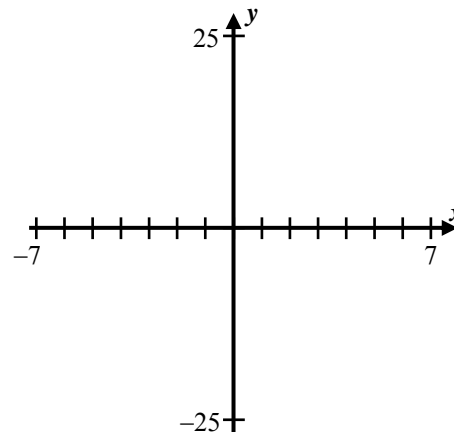


Clearly, a cubic may have one, two or three real roots and can have two turning points. Just as with parabolas, there exists a tie between a cubic's factors and its  $x$ -intercepts.

**Exercise #2:** Consider the cubic whose equation is  $y = x^3 - x^2 - 12x$ .

(a) *Algebraically* determine the zeroes of this function.

(b) Sketch a graph of this function on the axes below illustrating your answer to part (a).



**Exercise #3:** The largest root of  $x^3 - 9x^2 + 12x + 22 = 0$  falls between what two consecutive integers?

(1) 4 and 5

(3) 10 and 11

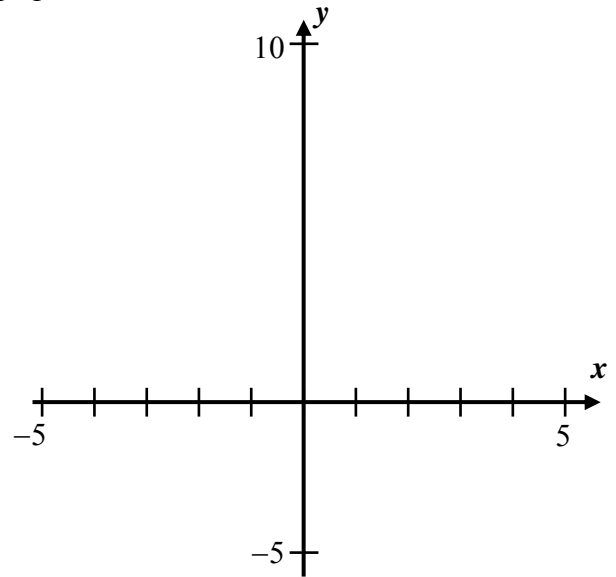
(2) 6 and 7

(4) 8 and 9

**Exercise #4:** Consider the quartic function  $y = x^4 - 5x^2 + 4$ .

(a) Algebraically determine the  $x$ -intercepts of this function.

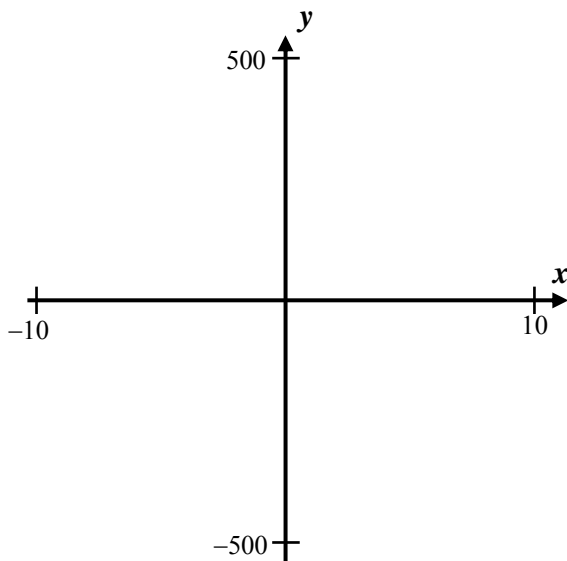
(b) Verify your answer to part (a) by sketching a graph of the function on the axes below.



**Exercise #5:** Consider the quartic whose equation is  $y = x^4 + 3x^3 - 35x^2 - 39x + 70$ .

(a) Sketch a graph of this quartic on the axes below. Label its  $x$ -intercepts.

(b) Based on your graph from part (a), write the expression  $x^4 + 3x^3 - 35x^2 - 39x + 70$  in its factored form.



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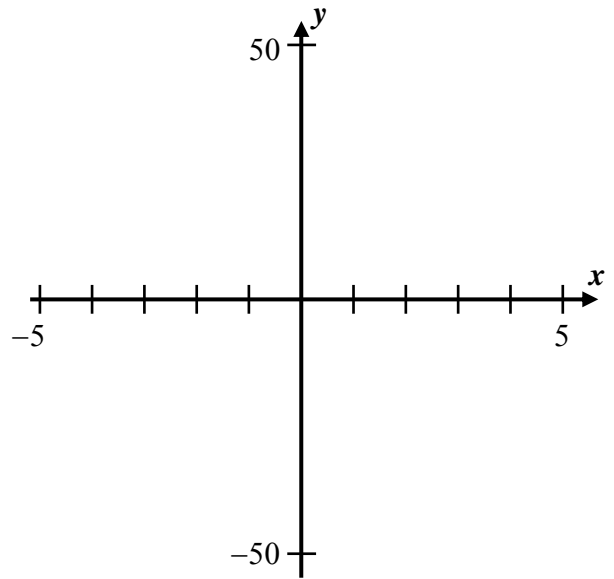
**GRAPHS AND ZEROS OF A POLYNOMIAL  
COMMON CORE ALGEBRA II HOMEWORK**

**FLUENCY**

1. Consider the cubic function  $y = x^3 + 2x^2 - 8x$ .

(a) Algebraically determine the zeroes of this cubic function.

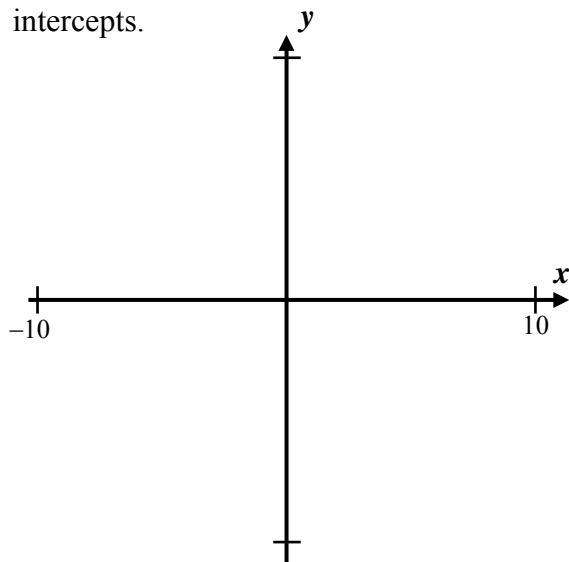
(b) Sketch the function on the axes given. Clearly plot and label each  $x$ -intercept.



2. Consider the cubic function  $y = x^3 + 2x^2 - 36x - 72$ .

(a) Find an appropriate  $y$ -window for the  $x$ -window shown on the axes and sketch the graph. Make the sure the window is sufficiently large to show the two turning points and all intercepts. Clearly label all  $x$ -intercepts.

(b) What are the solutions to the equation  $x^3 + 2x^2 - 36x - 72 = 0$ ?

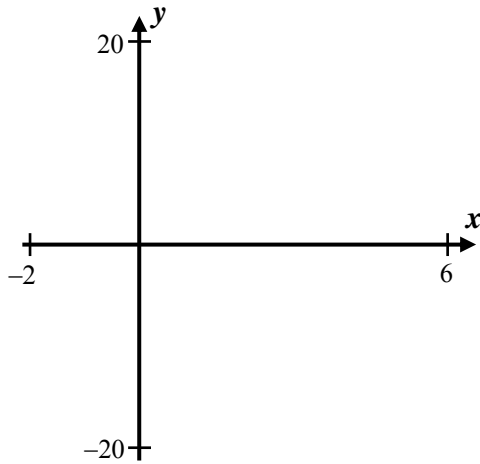


(c) Based on your answers to (b), how must the expression  $x^3 + 2x^2 - 36x - 72$  factor?



3. Consider the cubic function given by  $y = x^3 - 6x^2 + 12x - 5$ .

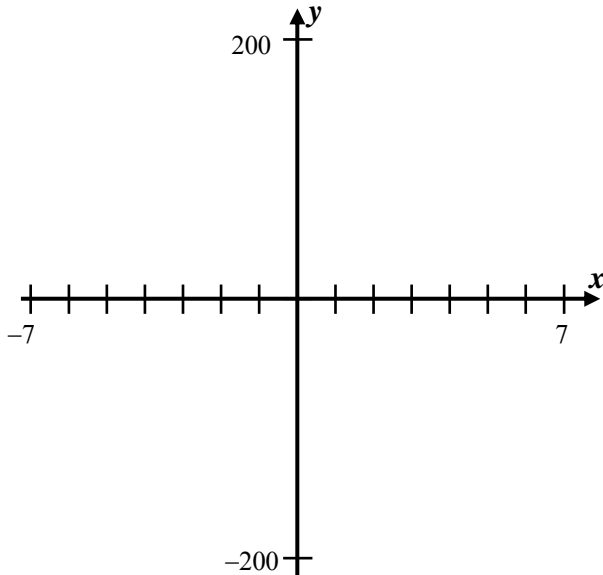
(a) Sketch a graph of this function on the axes given below.



(b) Considering the graphs of cubics you saw in class and those in problems 1 and 2, what is different about the way this cubic's graph looks compared to the others?

4. Consider the quartic function  $y = x^4 - x^3 - 27x^2 + 25x + 50$ .

(a) Sketch the graph of this function on the axes given below. Clearly mark all  $x$ -intercepts.



(b) Use your graph from part (a) to solve the equation  $x^4 - x^3 - 27x^2 + 25x + 50 = 0$ .

(c) Considering your answer to (b), how does the expression  $x^4 - x^3 - 27x^2 + 25x + 50$  factor?

5. In general, how does the number of zeroes (or  $x$ -intercepts) relate to the highest power of a polynomial? Be specific. Can you make a statement about the minimum number of zeroes as well as the maximum?

